

Anomalous asymmetry of the Fermi surface in the $\text{YBa}_2\text{Cu}_4\text{O}_8$ high temperature superconductor revealed by Angle Resolved Photoemission Spectroscopy

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We use microprobe Angle-Resolved Photoemission Spectroscopy (μ ARPES) to study the Fermi surface and band dispersion of the CuO_2 planes in the high temperature superconductor, $\text{YBa}_2\text{Cu}_4\text{O}_8$. We find a strong in-plane asymmetry of the electronic structure between directions along a and b axes. The saddle point of the antibonding band lies at a significantly higher energy in the a -direction ($\pi, 0$) than the b -direction ($0, \pi$), whereas the bonding band displays the opposite behavior. We demonstrate that the abnormal band shape is due to a strong asymmetry of the bilayer band splitting, likely caused by a non-trivial hybridization between the planes and chains. This asymmetry has an important implication for interpreting key properties of the Y-Ba-Cu-O (YBCO) family, especially the superconducting gap, transport and results of inelastic neutron scattering.

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It is commonly accepted that the conduction electrons/holes in the CuO_2 planes play an essential role in determining the electronic properties of the high- T_c superconductors. It is however not totally understood how the charge carriers arrange themselves and interact with each other. Strong a - b axis asymmetry of both the normal- and superconducting-state electronic properties have been observed in the Y-Ba-Cu-O (YBCO) family especially in $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$ (Y123) and $\text{YBa}_2\text{Cu}_4\text{O}_8$ (Y124), which possess double CuO_2 planes sandwiched between single and double CuO chains, respectively. The London penetration depth (λ) measured by muon-spin rotation shows a strong asymmetry ($\lambda_a/\lambda_b \approx 1.2$ in Y123^{1,2} and $\lambda_a/\lambda_b \approx 1.5$ in Y124³). Here the a - and b -axis directions are perpendicular to and along the chains, respectively. Angle Resolved Photoemission Spectroscopy⁴ observes a 50% larger gap along the chain direction in Y123. Angle-Resolved Electron tunneling in Y123/Au/Nb junctions also indicates a superconducting gap (Δ) asymmetry of $\Delta_b/\Delta_a \approx 1.5$ ⁵. Most recent reports using a similar technique, however, show only 20% difference⁶. Many theoretical models have been proposed in order to explain these results. These include the formation of striped phases⁷, orthorhombicity of the crystal structure⁸, proximity coupling between chains and planes⁹, broken time-reversal symmetry¹⁰, and an admixture of $d_{x^2-y^2} + s$ pair states¹¹. The spin dynamics in Y123, observed in inelastic neutron scattering (INS) experiments, also shows a significant a - b axis asymmetry in the vicinity of the wavevector $(1/2, 1/2)$ ^{12,14,15,16}. Mook *et. al.*¹³ report almost one-dimensional patterns and suggest that this is evidence for existing stripe phases⁷. In contrast, recent INS results on Y123 show that the spin

fluctuations are two-dimensional, although they have a strong a - b asymmetry¹⁶. In the latter case, a Fermi-liquid-based scenario might be more relevant for explaining the asymmetric spin dynamics^{8,17,18}.

Part of the controversy arises due to a lack of detailed band structure measurements in YBCO, since most ARPES experiments performed on this material have focused on $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$ (Y123) variety, which has fractional oxygen stoichiometry in the chains. These samples do not cleave well and suffer complications due to the ordering of oxygen in the chains. The resulting unstable sample surfaces makes ARPES spectra difficult to interpret⁴. Although band calculations predict a significant $a - b$ axis asymmetry of the band structure in CuO_2 planes due to a plane-chain coupling, that is often ignored when interpreting the electronic properties because of a lack of the experimental evidence supporting these predictions. Until now, there have been no observation of $a - b$ axis asymmetry in the Fermi surface of the CuO_2 planes by angle-resolved photoemission spectroscopy (ARPES) in YBCO^{4,19,20,21,22,23,24}. We chose $\text{YBa}_2\text{Cu}_4\text{O}_8$ (Y124) for studying the band structure by ARPES, because Y124 has a fixed oxygen stoichiometry that results in a much more stable surface than that of Y123 and avoids problems due to oxygen ordering in chains. We have previously demonstrated that the plane and chain bands can be distinguished by using both a small UV beam (50-100 μm) and a tunable incident photon energy²⁴. This lead to observation of significant differences in the momentum dependence of the bilayers splitting between Bi2212 and YBCO. Since it was sufficient for this purpose to acquire data only along nodal and a -axis directions, we could not make state-

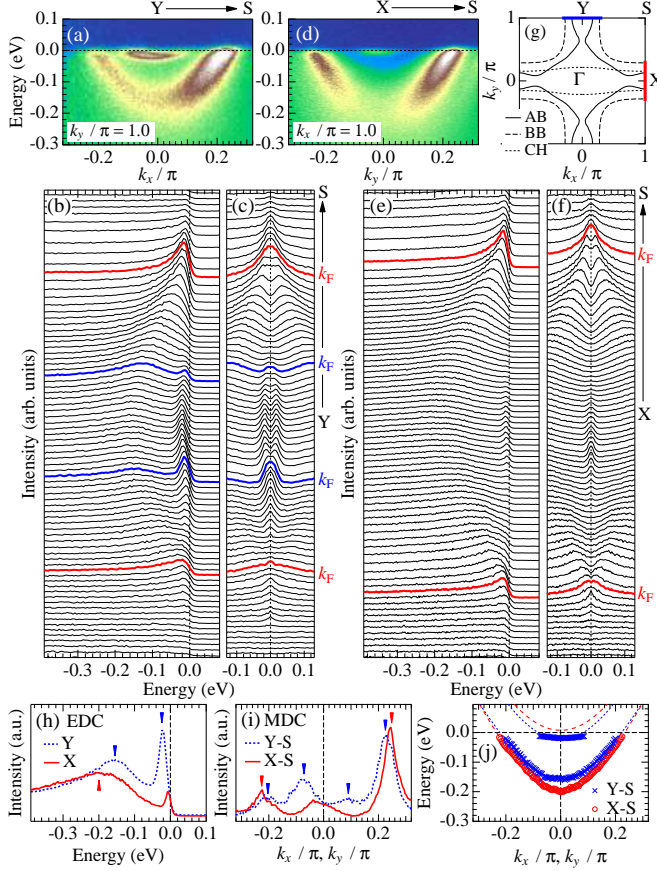


FIG. 1: (Color online) ARPES intensity of a plane domain and corresponding EDCs along Y-S (a,b) and X-S (d,e) indicated in (g). (c,f) Symmetrized EDCs of (b) and (e) close to the Fermi level. (g) Fermi surfaces of antibonding-, bonding-, and chain-band (AB, BB, and CH, respectively) obtained by band calculation²⁷. (h) EDCs at X and Y. (i) MDCs at the Fermi level along Y-S and X-S. (j) Band dispersions along Y-S and X-S determined from EDC peak positions of (b) and (e). Dotted blue lines and dashed red lines represent tight binding fits³³ along Y-S and X-S, respectively.

ments about the $a - b$ axis anisotropy. In this letter, we compare the band structure along a and b axis with much improved data quality due to use of high flux beamline and longer acquisition times. We found a small but a significant $a - b$ axis asymmetry in the band structure, which is mainly due to the variation of the bilayer band splitting being about 40% larger along the a -direction. Our results suggest that the coupling between the planes and chains and the consequent asymmetry of the band structure represents a crucial ingredient in our understanding of the origin of the asymmetries in the electronic and magnetic properties of YBCO systems.

Untwinned high quality single crystals of underdoped $\text{YBa}_2\text{Cu}_4\text{O}_8$ ($T_c \simeq 80\text{K}$) with a sharp superconducting transition ($\Delta T_c \simeq 3\text{K}$) were grown by the self-flux method under high oxygen pressure²⁵. The ARPES experiments were carried out using a Scienta SES2002

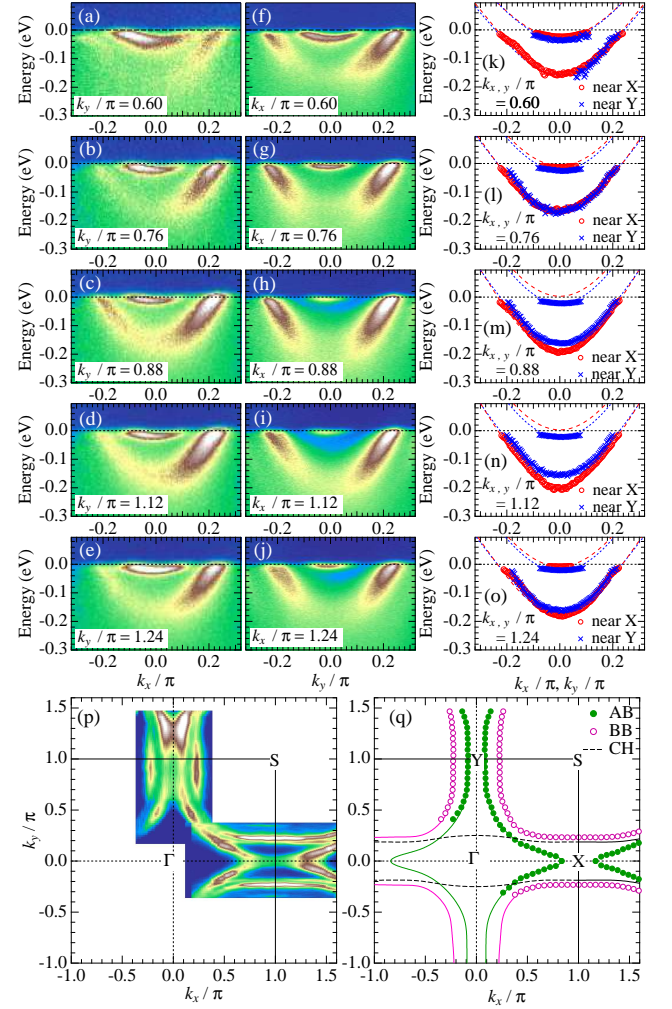


FIG. 2: (Color online) ARPES intensity at momentum cuts parallel to Y-S (a-e) and X-S (f-j). (k-o) Band dispersion determined from the EDC peak positions and tight binding fits³³. (p) ARPES intensity integrated within $\pm 10\text{meV}$ centered at the Fermi level as a function of k_x and k_y . (q) Fermi surface plots of antibonding-band (AB, green filled circle) and bonding-band (BB, purple open circle) determined from the peak position of the MDCs at the Fermi level.

hemispherical analyzer mounted on the SIS beamline of the Swiss Light Source (SLS). As a reference for the Fermi energy, we used the spectral edge position of evaporated Au in electrical contact with the sample. The energy and angular resolutions were 20 meV and 0.1° , respectively. All spectra were measured at 25K using a 33eV photon energy. In order to observe both a - and b -axis directions with an identical ARPES setting (photon polarization and geometry of analyzer and sample), we rotated the samples by 90° following the same micro-domain on the sample surface. We measured several samples and always obtained similar results.

Figures 1 (a,b) and (d,e) show ARPES data (intensity maps and corresponding energy distribution curves

(EDCs)) measured along Y-S and X-S, respectively. Those momentum cuts are illustrated in panel (g) along with the Fermi surface of the planes and chains obtained by band calculation²⁷. Around Y (chain direction), both dispersions of the antibonding (AB) and bonding (BB) bands, attributed to the CuO_2 bilayer splitting, are clearly observed at higher and lower energies, respectively. Note that, due to matrix element effects, the ARPES intensity at positive k_x is stronger than at negative k_x in the lower energy band. This k_x dependence becomes opposite for the higher energy band. Such anti-correlation is typical for bonding and antibonding bands due to the orthogonality of their wavefunctions²⁸. In contrast to the Y direction, the AB signal is very weak close to X (the direction perpendicular to the chains), whereas the BB is clearly seen. The difference between the two antinodal cuts is more clearly illustrated by plotting the EDCs taken at X and Y in Fig.1 (h), and the momentum distribution curves (MDCs) at the Fermi level in Fig.1 (i). We find that the BB dispersion around X displays a deeper bottom (by $\sim 40\text{meV}$) and a wider Fermi closing than that around Y. Although a large peak corresponding to an energy state of AB is seen below the Fermi level (around -20meV) in the EDC at Y (panel (h)), the peak edge of a weak AB signal appears to be pinned to the E_F at X. We used the symmetrization method²⁹ as well as the MDC peak position to determine the Fermi crossing points; EDCs are reflected about the Fermi level and added to the unreflected ones. This technique removes the Fermi function and enables us to immediately identify the Fermi crossing. The symmetrized EDCs of Fig. 1 (b) and (e) are plotted in the Fig. 1 (c) and (f), respectively. When the dispersion crosses E_F , two peaks in the symmetrized EDC due to presence of low-lying energy states merge into a single one at Fermi momentum. This is clearly seen both for AB and BB with moving away from Y along Y-S (panel (c)). The superconducting gap is not observed in these spectra because the YBCO sample surface is known to be overdoped after cleaving^{24,31}. Along X-S (panel (f)), the BB clearly shows a Fermi crossing. On the other hand, the symmetrized EDC very close to X has only one peak, which indicates that there is no Fermi crossing in AB along this cut. The shape of symmetrized EDC is sensitive to the value of experimental energy resolution³⁰. However we can confirm this from a behavior of the spectral intensities along Γ -X shown in Fig. 3(d); the intensity sharply decreases toward X, which indicates that the AB goes beyond E_F near X and only a small spectral tail is seen on the occupied side. In Fig. 1 (j), we summarize the AB and BB dispersions of the occupied states determined from the peak position of the EDCs in panels (b) and (e) along with tight binding fitting curves³³. Although our data represents the overdoped state, the band anisotropy reported here is expected to be valid for other doping levels because it is well known that doping of cuprates amounts to a rigid band shift³².

Figure 2 (a-e) and (f-j) show ARPES intensity maps

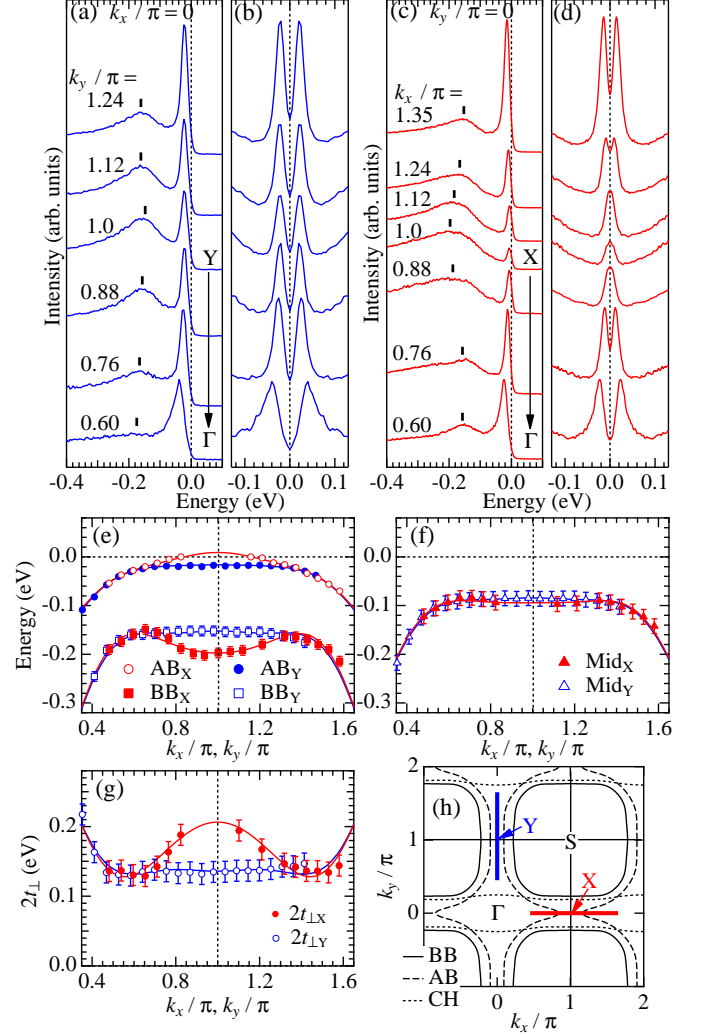


FIG. 3: (Color online) EDCs and the symmetrized ones measured at momenta along Γ -Y (a,b) and Γ -X (c,d) indicated in (h). (e) Dispersion of antibonding- and bonding-band along Γ -X (AB_X and BB_X) and Γ -Y (AB_Y and BB_Y) determined from peak positions of EDCs and symmetrized EDCs. Solid lines represent tight binding fits³³. (f) The midpoints of AB and BB along Γ -X (Mid_X) and Γ -Y (Mid_Y). (g) Energy of bilayer band splitting along Γ -X ($2t_{\perp X}$) and Γ -Y ($2t_{\perp Y}$). (h) Brillouin zone.

around Y and X measured along various momentum cuts parallel to Y-S and X-S, respectively. Around X (panel (f-j)), the ARPES intensity near E_F rapidly increases while moving away from the antinode due to the appearance of AB on the occupied side. This is in contrast to the strong intensity of the AB observed for all momentum cuts around Y (panels (a-e)). We determine both AB and BB dispersions from the EDC peak positions, and plot the results near Y and X in Fig. 2(k-o); each panel is for two momentum cuts at equal distance from X and Y. The difference in the dispersions between the two regions reaches a maximum close to the antinodes,

then decreases toward the nodes. The strong a - b axis asymmetry of the Fermi surfaces is further visualized in Fig. 2(p) by plotting the ARPES intensity integrated within ± 10 meV of E_F as a function of k_x and k_y . In Fig. 2(q), we plot the Fermi crossing points extracted from the MDC peak positions at E_F . We find an interesting topology of the Fermi surface which appears to be hole-like (centered around S) close to Y and electron-like (centered around Γ) close to X. We should note that the previously reported data²⁴ was consistent with hole-like Fermi surface close to X. This difference is most likely due to small variation of doping for different batches of samples. In the previous work, the data was measured only in X quadrant and reflected about symmetry planes to simply show the 2D character of Fermi surface that is different from 1D chain. In this work, we measured both X and Y directions on the same cleave to compare these in the same condition. We could get the same result for several samples cut out from a sample batch with high quality.

In order to understand what causes the significant a - b asymmetry, we carefully compare the band dispersions along Γ -Y and Γ -X. Figure 3 (a-b) and (c-d) show the EDCs and the corresponding symmetrized EDCs measured along Γ -Y and Γ -X, respectively (see panel (h)). We determined the energy states of BB (AB) along the two momentum cuts from the peak positions of the EDCs (symmetrized EDCs), and plot these in panel (e). We find that the BB along Γ -X has a convex downward dispersion centered at X. This is in contrast with all other dispersions (AB along Γ -X and both AB and BB along Γ -Y), which show a convex upward shape. We stress that the former band shape is specific to Y124 because the latter has been observed in many cuprates³² such as $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$ (Bi2212), $\text{Bi}_2\text{Sr}_2\text{CuO}_{6+\delta}$ (Bi2201), and $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ (LSCO). Figure 3(g) shows the splitting energy ($2t_\perp$, where t_\perp is the interlayer hopping integral within the bi-layers) estimated along Γ -X and Γ -Y. It is clear that $2t_\perp$ along Γ -X has a bump close to X and the difference from that along Γ -Y is about 40% (~ 60 meV). We therefore conclude that the characteristic band shape

close to X (the electron-like Fermi surface in AB and a convex downward dispersion in BB) is a result of an enhanced bilayer coupling around X, which pushes the AB up above E_F and pushes down the BB more than that around Y. In Fig. 3(f), we plot the mean-energies of AB and BB along Γ -X and Γ -Y. We find that the dispersion is almost identical along the both cuts, which indicates that the in-plane orthorhombicity of the Y124 crystal structure ($b/a \approx 1.008$)²⁵ causes only a negligible a - b axis asymmetry of the *in-plane* hopping integral ($t_{//}$). This small crystal orthorhombicity, therefore, is unlikely to cause a significant a - b asymmetry of the *interlayer* hopping (t_\perp). The enhanced bilayer coupling around X, where the Fermi surface of chains is adjacent to that of planes, is most likely due to a non trivial (momentum dependent) coupling between the chains and planes^{26,27}. It is worth noting that the current value of $2t_\perp$ (~ 160 meV) is about 4 times smaller than that estimated from band calculations (~ 600 meV)²⁷, which indicates that strong electron correlations suppress the interlayer hopping.

In conclusion, we find a strong in-plane a - b asymmetry of the electronic structure in $\text{YBa}_2\text{Cu}_4\text{O}_8$ (Y124). The Fermi surface in the antibonding band has a hole-like shape (centered around S) close to Y and an electron-like shape (centered around Γ) close to X. This asymmetry is caused by an enhanced bilayer band splitting close to X, where the Fermi surface of chains is adjacent to that of planes, likely due to a nontrivial coupling between the chains and planes. These results are crucial to understand the abnormal asymmetries observed in the superconducting gap and the significantly anisotropic spin dynamics, strongly supporting a number of recent theoretical works^{8,17,18}.

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